

## Parameterized Algorithms Tutorial

### Tutorial Exercise T1

You are given an  $n \times n$  matrix  $M$  and an integer parameter  $k$ . The goal is to select  $k$  non-zero entries  $S$  such that every other non-zero entry is either in the same row or same column as some element in  $S$ . Is this problem in FPT or W-hard? Justify your answer.

### Tutorial Exercise T2

Consider the following version of the STEINER TREE problem: an input is a graph  $G = (V, E)$ , a set  $S \subseteq V$  and an integer parameter  $k$ ; the goal is to decide whether there exists a set  $T \subseteq V \setminus S$  of size at most  $k$  such that  $G[T \cup S]$  is connected. Is this problem FPT or W-hard? Justify your answer as usual.

### Homework H1

You are given a graph  $G$  and a positive integer  $k$  as parameter. You have to decide whether there exists a vertex set  $S$  of size at most  $k$  such that  $G - S$  is  $r$ -regular, where  $r$  is a fixed positive integer selected in advance. Is this problem FPT or W-hard? Justify your answer.

### Homework H2

The DOMINATING SET problem is  $W[2]$ -complete in general but in many well-known graph classes it is fixed-parameter tractable. For instance, it has a linear kernel on the class of planar graphs (and, in fact, on graphs of bounded genus, on  $H$ -minor-free graphs etc.). A colleague claims that the problem is FPT on bipartite graphs. Would you agree with your colleague? Justify your answer.