

## Parameterized Algorithms Tutorial

### Tutorial Exercise T1

The INDEPENDENT SET problem is defined as follows. Given a graph  $G = (V, E)$  and an integer  $k$ , is there a set  $S$  of size  $k$  such that for all  $u, v \in S$ , where  $u \neq v$ , it holds  $uv \notin E(G)$ ? Is INDEPENDENT SET restricted to graphs of maximal degree  $d$ , where  $d$  is a constant, fixed parameter tractable parameterized by the size of the solution  $k$ ?

### Tutorial Exercise T2

The PLANAR INDEPENDENT SET is the INDEPENDENT SET problem restricted to planar graphs. Is PLANAR INDEPENDENT SET fixed parameter tractable parameterized by the solution size  $k$ ?

### Tutorial Exercise T3

The CLUSTER VERTEX DELETION PROBLEM is defined as follows: given a graph  $G = (V, E)$  and an integer parameter  $k$ , does there exist a set  $S$  of size at most  $k$  such that  $G[V \setminus S]$  consists of a collection of disjoint cliques. The cliques are disjoint in the sense that they do not share vertices and/or edges and there is no edge with one endpoint in one clique and the other in a different clique. Design an algorithm that runs in FPT-time w.r.t.  $k$  as parameter.

### Homework H1

The TRIANGLE VERTEX DELETION problem is defined as follows. Given a graph  $G = (V, E)$  and an integer parameter  $k$ , are there  $k$  vertices whose deletion results in a graph with no cycles of length three? Show that this problem is fixed-parameter tractable. What is the running time of your algorithm? Is there some easy way to improve the running time?

[10 points]

### Homework H2

This exercise is concerned with the fixed parameter tractable algorithm for the CLOSEST STRING problem. An input to this problem consists of  $n$  strings  $s_1, \dots, s_n \in \Sigma^L$  of length  $L$  each and an integer parameter  $k$ . The question is whether there exists a string  $s \in \Sigma^L$  such that  $d(s, s_i) \leq k$ , for all  $1 \leq i \leq n$ . Explain this algorithm and analyze its running time. You should probably start by asking yourself the following question: How many differences can there be between two strings  $s_1$  and  $s_2$ , such there can exist a string  $s$  such that  $d(s, s_1) \leq k$  and  $d(s, s_2) \leq k$ ?

[10 points]