Lehrgebiet Theoretische Informatik

Problem Set 7 09.12.2011

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Parameterized Algorithms Tutorial

Tutorial Exercise T18

Provide an FPT-reduction from Independent Set to Short Turing Machine Acceptance (STMA).

Tutorial Exercise T19

Provide an FPT-reduction from Dominating Set to Short Multi-Tape Turing Machine Acceptance.

Tutorial Exercise T20

Consider the following variant of Vertex Cover:

Half Partial Vertex Cover

Input: A graph G = (V, E), an integer k.

Parameter: The integer k.

Question: Can k vertices in G cover at least |E|/2 edges?

Show that Half Partial Vertex Cover is in W[1] by reducing it to STMA.

Homework H15

Show that:

- 1. HITTING SET \leq_{FPT} Dominating Set.
- 2. Dominating Set \leq_{FPT} Hitting Set.

Homework H16

Consider the following variant of HITTING SET:

Half 3-Hitting Set

Input: A finite universe U, a family $\mathcal{F} \subseteq 2^U$ of sets of size exactly three,

an integer k.

Parameter: The integer k.

Question: Can k elements of U hit at least $|\mathcal{F}|/2$ sets?

Show that Half 3-Hitting Set is in W[1].