

## Parameterized Algorithms Tutorial

### Tutorial Exercise T31

The problem RED-BLUE DOMINATING SET is defined as follows: given a graph  $G$  whose vertex set is partitioned into two color sets  $R \cup B = V(G)$  and an integer  $k$ , decide whether there exists a set of  $k$  red vertices that dominate all blue vertices.

Express the above problem as a  $\text{MSO}_1[L]$  formula, where  $L = \{\text{red}, \text{blue}\}$  is the set of allowed labels. Can this problem be expressed in  $\text{MSO}_2$  *without* labels? What does this mean for the logics  $\text{MSO}_1[L]$  and  $\text{MSO}_2$ ?

### Tutorial Exercise T32

Recall the definition of  $\text{MSO}_1$  and  $\text{MSO}_2$ . In the following, let  $G$  be a graph and  $A$  be some vertex subset of  $G$ . Which one of the following properties are expressible in either logic?

1.  $A$  forms a cycle
2.  $A$  forms an induced cycle
3.  $G$  has some hereditary graph property  $\mathcal{P}$  characterized by a finite set of forbidden subgraphs
4.  $G$  has some hereditary graph property  $\mathcal{P}$  characterized by an infinite set of forbidden subgraphs

What consequence do items 1 and 2 have for HAMILTONIAN CYCLE?

### Tutorial Exercise T33

Develop dynamic programming algorithms for the following problems on graphs of bounded treewidth:

- 3-COLORABILITY
- TRIANGLE PACKING (vertex disjoint)

State the running time of each algorithm.